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# Backtesting VaR under the COVID-19 sudden changes in volatility

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## Abstract

We analyze the impact of the COVID-19 pandemic on the conditional variance of financial returns. We look at this effect from a global perspective, so we employ series of major stock and sectorial indices. We use the popular Hansen's Skewed-t distribution with EGARCH extended to control for sudden changes in volatility. We oversee the COVID-19 effect on measures of downside risk such as the Value-at-Risk. Our results show that there is a significant sudden shift up in the return distribution variance post the announcement of the pandemic, which must be explained properly to obtain reliable measures for financial risk management.

**Keywords:** Backtesting; EGARCH; Monte Carlo; Skewed-t; Value-at-Risk

**JEL classification codes:** C22, C58, G17

## 1 Introduction

The COVID-19 pandemic has led to massive upheavals in financial markets causing sudden changes in volatility; see e.g. Zhang et al. (2020), Shehzad et al. (2020) and Goodell (2020) for new research on this issue. These type of abrupt changes have been extensively documented and modeled by GARCH-type models with sudden shift dummy variables; see, e.g., Lamoureux and Lastrapes (1990), Aggarwal et al. (1999) and Mikosch and Stărică (2004). Recent empirical studies have used this methodology to model recent stock market volatility shocks; see e.g. Malik et al. (2005), Kang et al. (2009), Ewing and Malik (2017) and Anjum and Malik (2020). This paper follows this literature to study the impact of the COVID-19 crisis on financial return time-varying variances. For this purpose we use the exponential GARCH (EGARCH) model of Nelson (1991) augmented with a sudden shift dummy variable to incorporate the COVID-19 effect on volatility. For the skewed and heavy-tailed distribution of the standardized returns, we employ the popular Skewed-t of Hansen (1994). Hereafter, this model is referred to as EGARCH-D-ST. In an empirical exercise for major stock and sectorial indices, we show evidence that incorporating the COVID-19 abrupt shift has an important impact on the accuracy of estimating volatility dynamics and forecasting future Value-at-Risk

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(VaR). In line with previous results, we also find clear evidence on that accounting for the sudden change reduces the persistence in the EGARCH model. The performance of the previous model is compared with that of the model without the dummy variable through the unconditional backtesting procedure of Kupiec (1995) for the pandemic period. Since the asymptotic distribution of the Kupiec’s backtesting test is not adequate for our small sample size, we have obtained Monte Carlo p-values according to Christoffersen (2011).

The remainder of the paper is organized as follows. In Section 2 we present the EGARCH-D-ST model for asset returns. Section 3 provides an empirical application to forecast the VaR of major stock and sectorial returns with a backtesting analysis. Section 4 gathers the conclusions.

## 2 Modeling asset returns

Let the asset return  $r_t$  be a process characterized by the sequence of conditional densities  $f(r_t|I_{t-1};\boldsymbol{\psi})$ , where  $I_{t-1}$  denotes the information set available prior to the realization of  $r_t$ ,  $\boldsymbol{\psi} = (\boldsymbol{\theta}, \boldsymbol{\xi})$  is the vector of unknown parameters such that  $\boldsymbol{\theta}$  is the subset characterizing both the conditional mean and variance of  $r_t$ , i.e.  $\mu_t(\boldsymbol{\theta}) = \mu(I_{t-1};\boldsymbol{\theta})$  and  $\sigma_t^2(\boldsymbol{\theta}) = \sigma^2(I_{t-1};\boldsymbol{\theta})$ , and finally,  $\boldsymbol{\xi}$  is the subset characterizing the shape of the distribution of the innovations,  $z_t$ . Thus, we assume that

$$r_t = \mu_t + \varepsilon_t, \quad \varepsilon_t = \sigma_t z_t. \quad (1)$$

So, equation (1) decomposes the return at time  $t$  into a conditional mean which is assumed to be constant,  $\mu_t = \mu$ , and the term  $\varepsilon_t$  defined as the product between the conditional standard deviation,  $\sigma_t$ , and the innovation (or standardized return),  $z_t$ , with zero mean and unit variance. It is assumed that  $\{z_t\}$  is a sequence of independent identically distributed random variables driven by the skewed-T (ST) distribution of Hansen (1994) with parameter set  $\boldsymbol{\xi} = (\lambda, v)$  where  $\lambda \in (-1, 1)$  and  $v > 2$  control, respectively, for skewness and kurtosis, and denoted as  $z_t \sim iid ST(\boldsymbol{\xi})$ . Let  $\sigma_t^2 = E[\varepsilon_t^2|I_{t-1}]$  be the EGARCH (1,1) conditional variance model (Nelson, 1991) augmented with an intercept dummy variable to account for changes due the COVID-19 pandemic. Thus,

$$\log(\sigma_t^2) = \omega + \delta D_t + \beta \log(\sigma_{t-1}^2) + \alpha \left| \frac{\varepsilon_{t-1}}{\sigma_{t-1}} \right| + \gamma \frac{\varepsilon_{t-1}}{\sigma_{t-1}}, \quad (2)$$

where  $D_t = 1$  if the return observation belongs to after the 31th of December 2019 as the starting date of the COVID-19 period when the first case was reported to the World Health Organization (WHO) by China (WHO, 2020).

## 3 Empirical application

### 3.1 Dataset and estimation

We analyze the time-series behavior of 17 major stock market and 27 world sector indices. The data employed were daily percentage log returns, which were computed as  $r_t = 100 \log(P_t/P_{t-1})$  from daily closing prices (in \$)  $\{P_t\}_{t=1}^T$  series. The time period used comprises from December 30, 2016 to May 25, 2020, for a total number of  $T = 887$  observations. Table 1 provides the list of the series. All data series were downloaded from Datastream. The world sectorial indices data are supplied by Morgan Stanley Capital International (MSCI) Barra. The MSCI world sector indices capture the large and mid-cap companies across 23 developed markets countries around the world. All securities in each index are classified in the corresponding sector as per the

Global Industry Classification Standard. The stock market indices analyzed are selected to represent major stock markets across the world. Table 1 also reports the standard deviations of daily returns before and after December 31, 2019. These statistics confirm that the pandemic has had a great influence on the stock markets and as a result, an increase in the volatility in all cases. This evidence suggests a possible structural change in the unconditional volatility that should be considered in modeling the conditional variance in the spirit of Lamoreux and Lastrapes (1990).

Table1: Stock and sectorial indices used in the empirical analysis

Name	$s_b$	$s_a$	Name	$s_b$	$s_a$	Name	$s_b$	$s_a$
Stock market indices								
ASX 200	0.65	2.59	MIB	0.98	3.02	S&P 500	0.72	3.06
AEX	0.72	2.41	HANG SENG	0.99	1.86	NASDAQ	1.07	3.05
CAC 40	0.79	2.79	IBEX 35	0.81	2.73	SMI	0.72	2.03
BOVESPA	1.22	4.03	KOSPI	0.75	2.29	TSX	0.88	2.23
DAX 30	0.84	2.71	FTSE 100	0.69	2.43	MOEX	0.53	3.07
EUROSTOXX 50	0.77	2.66	MEXICO IPC	0.84	1.91			
Sectorial indices								
Banks	0.80	3.46	Communication services	0.73	2.40	Hotels	0.66	3.35
Materials	0.77	2.59	Transportation	0.72	2.43	Insurance	0.64	3.00
Aerospace and defense	0.91	3.83	Media	0.83	2.80	IT services	0.98	3.31
Oil and gas	0.95	4.36	Health Care	0.70	2.20	Airlines	0.96	4.01
Utilities	0.58	2.82	Biotec	1.04	2.42	Pharmaceuticals	0.65	1.81
Financials	0.74	3.25	Chemicals	0.78	2.56	Retail	1.02	2.50
Industrials	0.69	2.65	Consumer services	0.66	3.34	Software	1.12	3.25
Real State	0.57	2.90	Food/beverage/tobacco	0.58	2.04	Tobacco	1.04	2.44
Information technology	1.04	3.19	Gas utilities	0.56	1.85	Water utilities	0.88	3.32

This table presents the names and sample standard deviations of the stock market and sectorial indices used in the empirical analysis of this article. Both  $s_b$  and  $s_a$  denote the sample standard deviations of the series before and after 31/12/2019, respectively.

The parameters of our EGARCH-D-ST model were estimated using maximum likelihood (ML). Table 2 presents the estimation results. The unconditional mean parameter,  $\mu$ , is not significant for many return series. The parameter estimates of the conditional variance equation (2) show that, for all series, the model correctly captures the asset returns stylized features of (i) clustering and high persistence in volatility, and (ii) asymmetric response of volatility to positive and negative shocks. Indeed, the parameter  $\beta$ , which is related to the persistence for the EGARCH, is rather high for all series with mean estimates of 0.944 and 0.958 for stock market and world sector indices, respectively. Also, asymmetric response,  $\gamma$ , is significant for all series. The ST asymmetry parameter,  $\lambda$ , is significant for 13 out of the 17 stock market indices, and 19 out of the 27 world sector indices. So, there is evidence for asymmetry for most standardized returns series. Note also that the ST degrees of freedom parameter,  $\nu$ , estimates indicate that the cross-sectional means for the stock market and sectorial indices exhibit kurtosis levels of 6.2 and 7.1, which are far away from the Normal distribution (i.e., large value of  $\nu$ ). In short, the previous results suggest that the standardized returns are not normally distributed.

The dummy parameter, denoted as  $\delta$ , is significant for 15 and 25 stock market and world sector indices, respectively, indicating an important due-to-COVID sudden change in volatility across international markets and sectors. In order to analyse more precisely when the shift in volatility starts to become relevant, we estimate our model for four different subsamples across the whole sample period. The results, presented in Table 2 (Panel 2), indicate that for most of the series the sudden change dummy variable effects kicks in March 2020 as  $\delta$  becomes statistically significant. Only for a few stock market indices the effect is relevant already

in January and February, whilst for the world sectorial indices the break is apparent for 10 series already in February. We find that the magnitudes of the dummy coefficients become larger as well as significant at lower levels as we move through the OOS period. Figure 1 shows the plots of coefficient estimates and t-statistics over the OOS period for Nasdaq and Banks return series as representative examples.

Table 2: Estimation results

Cross-sectional distribution								
Panel 1: sample period 02/01/2017-26/05/2020								
	$\mu$	$\omega$	$\delta$	$\alpha$	$\gamma$	$\beta$	$\nu$	$\lambda$
Stock market indices								
Mean	0.020	-0.095	0.093	0.095	-0.171	0.944	6.190	-0.141
Q1	0.002	-0.111	0.072	0.058	-0.220	0.941	4.907	-0.175
Median	0.010	-0.095	0.083	0.094	-0.174	0.946	5.705	-0.142
Q3	0.038	-0.064	0.107	0.115	-0.128	0.958	6.370	-0.093
$M$	2	14	15	17	17	17	17	13
Sectorial indices								
Mean	0.034	-0.136	0.082	0.147	-0.112	0.958	7.105	-0.115
Q1	0.018	-0.078	0.062	0.118	-0.127	0.953	5.275	-0.016
Median	0.030	-0.132	0.071	0.149	-0.106	0.955	6.704	-0.133
Q3	0.062	-0.104	0.096	0.177	-0.087	0.964	8.918	-0.078
$M$	8	26	25	25	27	27	27	19
Panel 2: EGARCH Dummy significance over time								
Sample ends	31/01/2020	28/02/2020	30/03/2020	31/04/2020	26/05/2020			
Stock market	4 [5]	3 [7]	16 [17]	15 [16]	15 [16]			
Sectorial	3 [6]	10 [15]	26 [26]	25 [27]	25 [26]			

The rows present the mean, median, 25 and 75 percentiles (Q1 and Q3, respectively) from the cross-sectional distribution of the parameter estimates listed in the columns.  $M$  denotes the number of series with significant parameter at 5% level. There are 17 stock market and 27 sectorial indices. Panel 2 reports number of series for which the dummy variable parameter is significant at 5% (10% in brackets) for the several samples ending on 31/01/2020, 28/02/2020, 30/03/2020, 31/04/2020 and 26/05/2020.

### 3.2 Backtesting VaR

For the out-of-sample (OOS) analysis, we are interested in the VaR-backtesting performance comparison between the EGARCH-D-ST model, which does consider the sudden change in volatility due to the COVID-19 effect, and the EGARCH-ST model which is nested in the former when  $\delta = 0$  in (2) and does not account for the previous effect.

The backtest implementation involves the first  $T - N$  observations for the first in-sample window and the OOS period of length  $N = 81$  from February 3, 2020 to May 25, 2020, using a constant-sized rolling window. For every window we estimate the model parameters by ML and obtain a one-day-ahead forecast of the conditional variance,  $\sigma_{t+1}^2$ . We have done this for all return series presented above under several coverage levels (denoted as  $\alpha$ ): 1%, 2.5%, 5%. The one-day-ahead VaR for the  $\alpha$ -quantile is given by  $VaR_{t+1}(\alpha) = \mu + \sigma_{t+1} F_z^{-1}(\alpha; \boldsymbol{\xi})$  where  $F_z^{-1}(\alpha; \boldsymbol{\xi})$  represents the  $\alpha$ -quantile of the  $ST(\boldsymbol{\xi})$  distribution for the random variable  $z_t$  obtained through the inverse of its cumulative distribution function (cdf), and denoted as  $F_z(\cdot; \boldsymbol{\xi})$ . Let

$$h_{t+1}(\alpha) = \mathbf{1}(r_{t+1} < VaR_{t+1}(\alpha)) \quad (3)$$

denote the violation or hit variable. We obtain the quadratic loss function, which incorporates the exception magnitude and provides useful information to discriminate among similar models in terms of

the unconditional coverage criterion. Thus,

$$QL_{t+1}(\alpha) = (r_{t+1} - VaR_{t+1}(\alpha))^2 \times h_{t+1}(\alpha). \quad (4)$$

We estimate the sample averages for the daily estimations of (3) and (4) corresponding to the daily violations in (3) and the daily quadratic losses in (4) for the OOS period of  $N = 81$  days. The probability  $P(r_{t+1} < VaR_{t+1}(\alpha) | I_t) = \alpha$  suggests that violations are Bernoulli variables with mean  $\alpha$ . The null hypothesis for the unconditional backtest,  $H_0 : E[h_{t+1}(\alpha)] = \alpha$ , corresponds to the following likelihood ratio (LR) test statistic initially proposed by Kupiec (1995):

$$LR_U(\alpha, \hat{\pi}) = -2 \ln [L(\alpha) / L(\hat{\pi})] \stackrel{a}{\sim} \chi_1^2, \quad (5)$$

where  $L(\alpha)$  is the likelihood of an *i.i.d.* Bernoulli ( $\alpha$ ) hit sequence, i.e.  $L(\alpha) = (1 - \alpha)^{N_0} \alpha^{N_1}$  such that  $N_0$  and  $N_1$  are the number of zeroes and ones (or hits) in the sample, and  $\hat{\pi} = N_1/N$  is the sample average of the hit sequence in (3) for the whole OOS period such that  $\hat{h}_{t+1}(\alpha) = \mathbf{1}(r_{t+1} < \widehat{VaR}_{t+1}(\alpha)) = \mathbf{1}(\hat{u}_{t+1} \leq \alpha)$  with  $\widehat{VaR}_{t+1}(\alpha)$  and  $\hat{u}_{t+1}$  as the estimations of  $VaR_{t+1}(\alpha)$  and  $u_{t+1} = F_z\left(\frac{r_{t+1} - \mu}{\sigma_{t+1}}; \boldsymbol{\xi}\right)$ . Hence, we can easily obtain  $L(\hat{\pi}) = (1 - \hat{\pi})^{N_0} \hat{\pi}^{N_1}$ .

Finally, as our OOS period is short, we perform a simulation exercise to check the robustness of our number of violations respecting the sample size. For this purpose, we follow Christoffersen (2011) so as to obtain the Monte Carlo simulated p-values since they are more reliable than those under the  $\chi^2$  distribution for small sample sizes. The simulated p-values are obtained as follows. First, we generate 9999 samples of random *i.i.d.* Bernoulli ( $\alpha$ ) variables with sample size  $N = 81$ . Second, we calculate 9999 simulated test statistics according to (5) and denoted as  $\{LR_U(\alpha, \hat{\pi}_i)\}_{i=1}^{9999}$ , where  $\hat{\pi}_i$  corresponds to the simulated  $i$ -th sample. Finally, the simulated p-value is given by

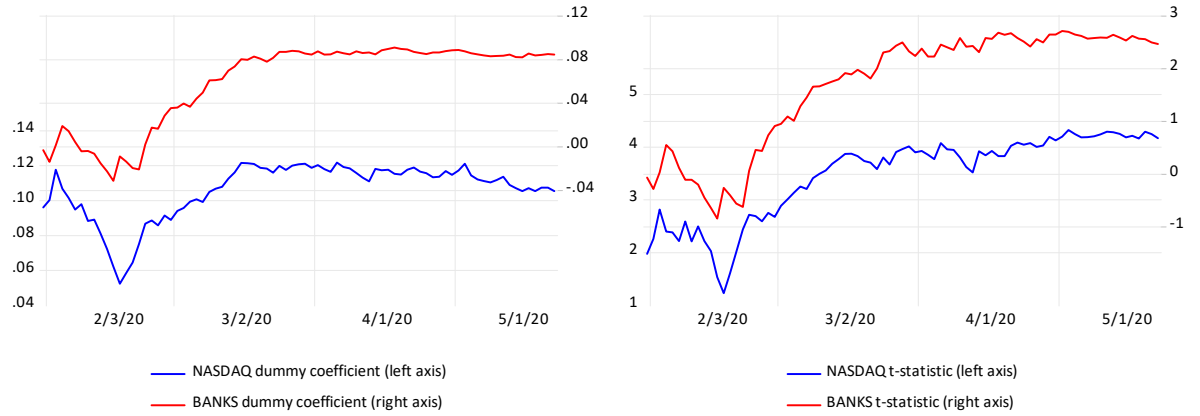
$$P\text{-value} = \frac{1}{10000} \left\{ 1 + \sum_{i=1}^{9999} \mathbf{1}(LR_U(\alpha, \hat{\pi}_i) > LR_U(\alpha, \hat{\pi})) \right\}. \quad (6)$$

Table 3 exhibits a descriptive analysis of VaR average violations (VIOL) and quadratic losses (MSE) obtained from EGARCH-D-ST and EGARCH-ST models through the OOS period. As a way to summarize the results across all indices, we report the mean, median, 25% and 75% percentiles (Q1 and Q3, respectively) of the cross-sectional distribution of each return index type. Our results clearly show that the EGARCH-D-ST delivers a number of violations closer to the theoretical ones, according to the unconditional backtest test results by using (6), as well as lower MSE values, for all three confidence levels and both index types. As an example, Figure 2 exhibits, for the KOSPI index at the top left, daily 1% VaR forecasts,  $\widehat{VaR}_{t+1}(0.01)$ . This plot shows that the number of violations over  $N = 81$  are 0 and 3 for the EGARCH-D-ST and EGARCH-ST, respectively. The figure also exhibits series plots related to the computation of the VaR series. The top-right plot shows that the one-period-ahead conditional volatility forecasts are higher under the EGARCH-D-ST. The plots at the bottom are for the parameters implied in the ST distribution for the standardized returns. The  $\lambda$  parameter, plots at the bottom right, and the  $v$  parameter, bottom left, both control predominantly for the skewness and kurtosis, respectively. It is observed that the  $v$  estimates are higher under the EGARCH-D-ST, and the  $\lambda$  series are negative and verify that the size of  $\lambda$  is higher under the EGARCH-ST. The corresponding skewness and kurtosis series under the ST distribution, which are obtained by plugging  $\lambda$  and  $v$  into the higher-order moment closed-form expressions in Jondeau and Rockinger (2003), show higher daily levels of both negative skewness and kurtosis under the EGARCH-ST model.<sup>1</sup> This evidence of higher kurtosis levels due to not considering shift dummies are, for instance, in line with that in Ewing and Malik (2017) and Anjum and Malik (2020). Figure 3 clearly illustrates the relation between persistence in volatility

<sup>1</sup>These series are not presented to save space.

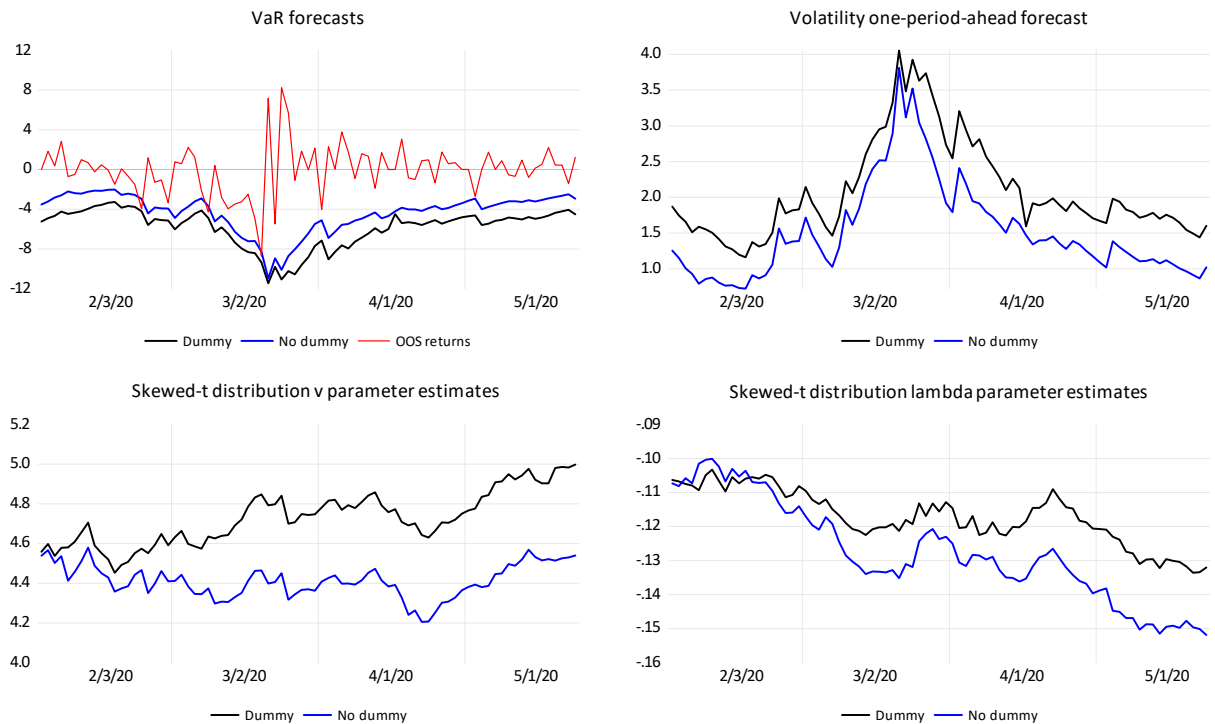
and sudden changes. The left plot shows that daily volatility autocorrelations (using the absolute return as a proxy for the volatility) are much higher for the whole sample, which includes the COVID-19 sudden change in volatility. The right plot shows that including sudden shift dummies reduces the persistence in the EGARCH-D-ST model.

Figure 1: Dummy coefficient over the out-of-sample period



This figure presents the dummy variable coefficient estimates together with their t-statistics over the OOS period: February 3, 2020 to May 25, 2020. Series: NASDAQ, BANKS. Observations 81.

Figure 2: VaR and volatility forecasts and Skewed-t parameter estimates. Series: KOSPI



This figure presents 1% VaR and volatility forecasts, as well as Skewed-t parameter estimates over the OOS period: February 3, 2020 to May 25, 2020. Series: KOSPI. Observations 81.

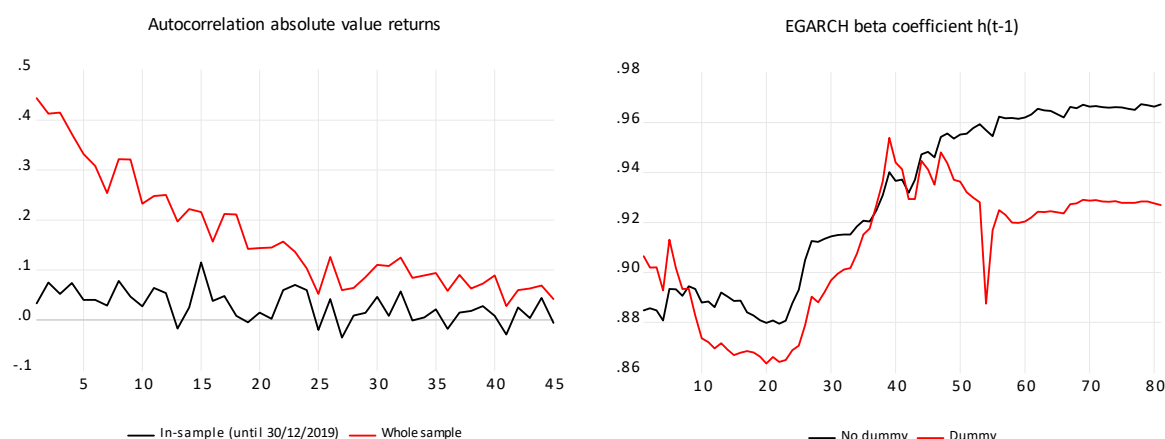
Table 3: Descriptive analysis of violations and MSE

$\alpha$		VIOL		MSE	
		EGARCH-D-ST	EGARCH-ST	EGARCH-D-ST	EGARCH-ST
Stock market indices					
0.01	Mean	2.9	4.1	0.268	0.405
	Q1	2	3	0.024	0.083
	Median	3	4	0.167	0.262
	Q3	4	5	0.382	0.518
	$m$	2 [12]	7 [15]		
0.025	Mean	4.8	7.5	0.585	0.787
	Q1	4	7	0.091	0.184
	Median	5	8	0.418	0.705
	Q3	7	8	0.772	0.942
	$m$	4 [6]	14 [16]		
0.05	Mean	8.4	11.8	0.974	1.250
	Q1	7	10	0.264	0.550
	Median	8	11	0.767	1.085
	Q3	10	13	1.210	1.442
	$m$	6 [8]	17 [17]		
Sectorial indices					
0.01	Mean	2.7	4.0	0.240	0.354
	Q1	2	3	0.011	0.056
	Median	3	4	0.069	0.175
	Q3	4	5	0.309	0.490
	$m$	3 [15]	11 [24]		
0.025	Mean	4.7	7.0	0.481	0.681
	Q1	4	6	0.086	0.258
	Median	5	7	0.342	0.507
	Q3	6	8	0.657	0.823
	$m$	3 [9]	17 [25]		
0.05	Mean	7.3	9.6	0.847	1.152
	Q1	6	8	0.305	0.600
	Median	7	10	0.672	0.847
	Q3	9	11	0.942	1.312
	$m$	3 [7]	15 [18]		

This table presents a descriptive analysis of one-day-ahead VaR forecasting performance from EGARCH-D-ST and EGARCH-ST models. Both VIOL and MSE denote, respectively, average violations and quadratic losses. The coverage level is  $\alpha = \{0.01, 0.025, 0.05\}$ . For each  $\alpha$  we present the mean, median, 25 and 75 percentiles (Q1 and Q3, respectively) for VIOL and MSE across the out-of-sample period.  $m$  denotes the number of times the null of the unconditional backtest is rejected according to equation (6) at 1% and (in brackets) at 5% levels. The data consists of daily return series from stock market and sectorial indices. Total sample: 887 observations from January 2, 2017 to May 25, 2020. OOS period: February 3, 2020 to May 25, 2020. Predictions: 81.



Figure 3: Volatility autocorrelation and persistence. Series: KOSPI



The left plot of this figure exhibits the autocorrelation of absolute value returns for both the whole sample and subsample up to 30/12/2019. The right plot presents the beta parameter estimates from EGARCH-ST and EGARCH-D-ST models for the OOS period: February 3, 2020 to May 25, 2020. Series: KOSPI. Observations 81.

## 4 Conclusions

In this paper we have investigated the sudden change in volatility of major stock and sectorial indices caused by the COVID-19 pandemic. Using the popular EGARCH with Hansen’s Skewed  $t$  distribution augmented with a sudden change dummy variable, we show the importance of incorporating the abrupt volatility shift for explaining volatility dynamics, forecasting VaR and backtesting. In addition, we confirm that when these changes are accounted for the persistence in volatility diminishes considerably.

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